

Homework - Distance:

1. Find the distance between the parallel lines:

$$\text{a) } \begin{aligned} \ell_1 : & 5x - 2y + 25 = 0 \\ \ell_2 : & 5x - 2y - 5 = 0 \end{aligned} \quad \left\{ \frac{30\sqrt{29}}{29} \right\}$$

$$\text{b) } \begin{aligned} \ell_1 : & 2x - y + 14 = 0 \\ \ell_2 : & 2x - y + 3 = 0 \end{aligned} \quad \left\{ \frac{11\sqrt{5}}{5} \right\}$$

2. Find the distance between:

$$\text{a) the point } A(-6,5,-3) \text{ and the line } (x,y,z) = (6,1,3) + t(5,-3,3) \quad \{2.76\}$$

$$\text{b) the lines } \begin{aligned} \ell_1 : & \vec{r} = (1,6,-2) + t(1,-2,5) \\ \ell_2 : & \vec{r} = (3,-4,-9) + k(-2,7,1) \end{aligned} \quad \{0.387\}$$

$$\text{c) the point } A(-1,8,-4) \text{ and the line } (x,y,z) = (3,-4,0) + t(-2,7,3) \quad \{8.53\}$$

$$\text{d) the lines } \begin{aligned} \ell_1 : & \vec{r} = (3,-5,2) + t(-3,-1,4) \\ \ell_2 : & \vec{r} = (3,3,-1) + k(2,3,-9) \end{aligned} \quad \{6.4\}$$

$$\text{e) the lines } \begin{aligned} \ell_1 : & \vec{r} = (4,-2,4) + t(-3,-1,4) \\ \ell_2 : & \vec{r} = (3,7,-1) + k(6,2,-8) \end{aligned} \quad \{9\}$$

$$\text{f) the lines } \begin{aligned} \ell_1 : & \vec{r} = (7,1,-3) + t(-1,4,2) \\ \ell_2 : & \vec{r} = (-3,6,-5) + k(-2,8,4) \end{aligned} \quad \{9.84\}$$