

## Vector Applications - Forces

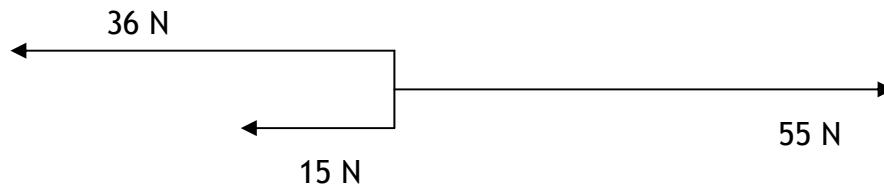
Recall: Resultant is the sum of 2 or more vectors  $\rightarrow \vec{R}$

Equilibrant is the opposite vector to the resultant  $\rightarrow \vec{E} = -\vec{R}$

Force:

- a vector quantity,
- a push or a pull
- measured in newtons ( $1\text{N} = 1\text{Kg}\cdot\text{m}/\text{s}^2$ )
- $\vec{F} = m\vec{a}$
- $\vec{F}_g = m\vec{g}$ ,  $\vec{g} = 9.8\text{m}/\text{s}^2$  [down]

Ex 1: Find the resultant of the following forces:



remember: East/right is positive

$$\begin{aligned}\vec{R} &= 55 + (-36) + (-15) \\ &= 4\text{N}[\text{right}]\end{aligned}$$

Ex 2: Find the equilibrant of three forces, one of 115N acting west, the other of 220N acting East, and the third of 105N acting East

$$\begin{aligned}\vec{R} &= 220 + 105 + (-115) \\ &= 210\text{N}[\text{E}]\end{aligned}$$

$$\begin{aligned}\vec{E} &= -\vec{R} \\ &= -210[\text{E}] \\ &= 210[\text{W}]\end{aligned}$$

**Note:** forces in equilibrium cause a net change of zero

∴ in 1-D the forces “cancel out”

2-D the addition of forces forms a closed  $\Delta$

### Force Question

Find the magnitude and direction of the equilibrant of two forces of 80 N and 50 N which act on the same object at an angle of 70 degrees to each other.

### Hanging Object Question

A sign with a mass of 100 kg is suspended from 2 wires which are attached to a ceiling. One wire makes an angle of 43 degrees with the ceiling and the other one makes an angle of 60 degrees with the ceiling. Find the tensions in the wires.

### Many Vector Questions

When asked to find the resultant or equilibrant of more than two vectors you should use algebraic vectors.

Find the resultant of the following forces:

58 N at  $S25^\circ W$

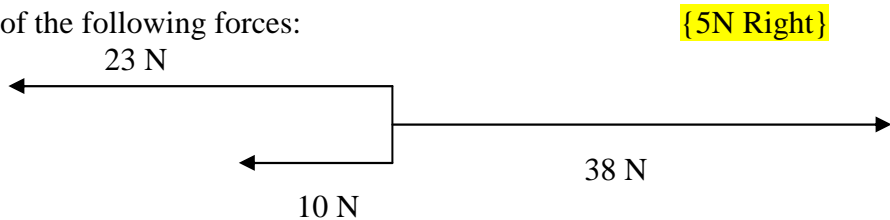
34 N at  $E10^\circ S$

40 N at  $N40^\circ W$

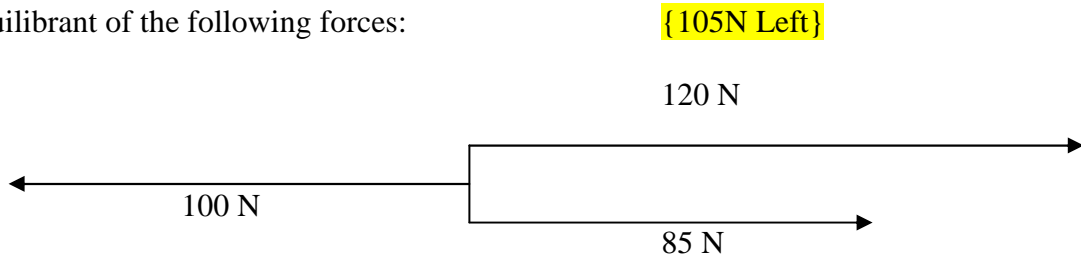
68 N at  $N55^\circ E$

## Vector Applications - Forces

1. Find the resultant of the following forces:



2. Find the equilibrant of the following forces:



3. Forces of 15 N and 23 N act at a point at an angle of 130 degrees to each other. Find the magnitude and direction of the resultant. **{17.62 N, 40.7° to 23N force}**
4. An object of mass 5kg is suspended from a horizontal ceiling by two strings making angles of 35 degrees and 62 degrees with the ceiling. Calculate the tensions in these strings. **{35 degree string has a tension of 23N and the 62 degree string has a tension of 40N}**

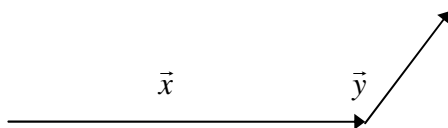
5. Determine the resultant of the following forces:

25 N acting S30° W  
 13 N acting N25° W  
 11 N acting SE

17 N acting N70° E  
 30 N acting E

**{37.7 N acting S72° E}**

6. Given :  $|\vec{x}| = 9$  and  $|\vec{y}| = 4$  as illustrated, determine  $|3\vec{x} - 2\vec{y}|$  given that  $|\vec{x} + 2\vec{y}| = 15$ .



**{23.5}**